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**WEIGHTED ERROR/ERASURE CORRECTION IN A MULTI-TRACK STORAGE  
MEDIUM**

**1. Field of the Invention:**

5       The present invention relates generally to the application of error correcting codes to storage media. Specifically, the present invention provides a method, computer program product, and data processing system for correcting errors and erasures in a storage medium having  
10 multiple tracks of data.

**2. Background of the Invention:**

15       Error correcting codes (ECCs) play a vital role in today's world. As storage systems pack more and more information into smaller physical spaces, as wireless and other communications systems transmit data over cluttered communications media, as our technology pushes the limits of physics, there is an ever-increasing need to be protected from data errors. Compact discs, magnetic  
20 tapes and disks, memory chips, and satellite transmissions are among the many technologies that are prone to error from physical forces, yet we take these things for granted. The Voyager spacecraft developed by NASA in the 1970s, for instance, transmits radio signals  
25 to Earth with less power than emitted by an ordinary 60-watt light bulb, yet it has captured some of the clearest pictures of the outer planets taken to date.

30       A remarkable technology makes all of this reliability possible. All of these technologies rely, at least in part, on the use of error-correcting codes.

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Error correcting codes add a sufficient level of redundancy to a piece of data to be able to recover the data should the data become corrupted. Many such error correcting codes have been developed, such as Hamming  
5 codes, which are described in Hamming, R.W., Error detecting and error correcting codes, *Bell System Tech. J.*, 26 (1950), pp. 147-160.

Many modern applications that make use of error correcting codes use what are known as Reed-Solomon  
10 codes, including the Voyager spacecraft and compact discs (which use a variant of Reed-Solomon codes known as CIRC, Cross-Interleaved Reed-Solomon Codes). Reed-Solomon codes were first described in Reed, I.S. and G. Solomon, Polynomial Codes over Certain Finite Fields, *J. Soc. Ind. Appl. Math.*, 8 (1960), pp. 300-304.  
15

The Reed-Solomon codes are part of a family of codes known as Bose-Chaudhuri-Hocquenghem (BCH) codes. BCH codes have the desirable property that they can correct a large number of errors with a minimum of redundant  
20 information; BCH codes can also correct a larger number of errors if the locations of the errors are known in advance. Errors with known locations are called "erasures" in the art. Also, in the art, an "error" is an error with an unknown location. Several algorithms,  
25 such as the Berlekamp-Massey algorithm, are known to those skilled in the art for efficiently decoding BCH codes to recover erasures and errors. Several of these algorithms are described in Blahut, Richard E., The Theory and Practice of Error Correcting Codes, Addison-  
30 Wesley, Reading, MA (1983), pp. 161-206.

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Mathematically, a Reed-Solomon code maps values from a vector space of a first dimension over a finite field to a vector space of a second, higher dimension over the same field. The values in the second vector space  
 5 correspond to coefficients of a set of linear equations, the solution to which is the data to be recovered. The element of redundancy in a Reed-Solomon code stems from the fact that the number of linear equations provides exceeds the minimum number "m" needed to recover the  
 10 data, and that any "m" of the equations are linearly independent. In other words, you can recover the data by solving any "m" of the equations as a system.

Algorithms such as the Berlekamp-Massey algorithm described previously, perform this decoding step  
 15 efficiently, taking into account the known locations of erasures (that is, which of the linear equation coefficients have been corrupted) so as to be able to recover a greater amount of data when erasures can be identified.

20 In any Reed-Solomon code, the entire vector of data can be recovered only if

$$2t + e \leq n - m$$

where "t" is the number of errors, "e" is the number of erasures, "n" is the number of linear equations available  
 25 to choose from (i.e., the dimension of the second vector space), and "m" is the is the minimum number of linear equations necessary to recover the data. In other words, it takes one more uncorrupted linear equation to *find* an error than it does to simply correct one.

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Reed-Solomon codes, because they rely on the use of multiple sets of coefficients, are easily adapted for use in multi-track recording media, such as magnetic tape. An encoded vector of data can be made to span multiple  
5 tracks, such that the coefficients for each of the Reed-Solomon equations reside on a separate track. In that way, if one or more tracks become corrupted, but at least "m" tracks can be read successfully, the entire original vector of data can be recovered. Of course, identifying  
10 those "m" tracks is easier when some of the corrupted tracks are already known.

Error detecting codes provide a way of identifying errors in a stream of data. One very effective error-detecting code is the cyclic redundancy check (CRC). CRC  
15 codes are described in Messmer, Hans-Peter, The Indispensable PC Hardware Book, 2d. Ed., Addison-Wesley, Reading, MA (1995), pp. 694-702. An erasure on a particular track can be identified by interposing CRC codes on each track at periodic intervals. The CRC codes  
20 act as a sort of checksum for the data they follow. An erasure can be identified by comparing a CRC code calculated from a block of data on a given track with the CRC code recorded at the end of the block.

While this is an accurate way to identify a track  
25 containing corrupted data, it says nothing about the location within the block of data or the extent of the corruption. Thus, a section of magnetic tape with small amounts of corruption on all or most of the tracks will appear as all containing erasures simultaneously, when in  
30 fact, there may only be isolated incidents of corruption

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on different tracks at different times. If, in such a situation, all of the tracks known to contain errors are treated as erasures, no data will be recovered, since the erasure tracks will be disregarded as corrupted, and  
5 there will not be enough remaining tracks to be able to recover the data.

Thus, while identification of erasures is helpful when large amounts of data on a given track are corrupted, it can cause problems when small errors are  
10 randomly distributed across many of the tracks. It would, thus, be desirable to have a system for correcting errors in a multi-track medium that is adapted to handle both large erasures and small errors.

**SUMMARY OF THE INVENTION**

The present invention provides a method, computer  
5 program product, and data processing system for  
recovering corrupted data in a multi-track storage  
medium, such as magnetic tape, using a Reed-Solomon or  
other similar error correcting code system. A correction  
history keeping a tally of actual corrected instances of  
10 corruption in the storage medium is established. The "N"  
tracks requiring the greatest number of actual error  
corrections are designated as erasures. Any errors in  
the remaining tracks must be found on an individual basis  
before being corrected.

**BRIEF DESCRIPTION OF THE DRAWINGS**

The novel features believed characteristic of  
5 the invention are set forth in the appended claims. The  
invention itself, however, as well as a preferred mode of  
use, further objectives and advantages thereof, will best  
be understood by reference to the following detailed  
description of an illustrative embodiment when read in  
10 conjunction with the accompanying drawings, wherein:

**Figure 1** is an external view of a data processing  
system in which the processes of the present invention may  
be performed;

**Figure 2** is a block diagram of such a data processing  
15 system;

**Figure 3** is a diagram depicting multi-track magnetic  
tape;

**Figure 4** is a diagram depicting a process of error  
correction in accordance with a preferred embodiment of  
20 the present invention;

**Figure 5** is a diagram illustrating how the processes  
of a preferred embodiment of the present invention may be  
applied to a multi-track data storage medium to maximize  
error-correcting capabilities;

**Figure 6** is a diagram depicting a process of  
25 decoding one block of Reed-Solomon encoded data from a  
multi-track magnetic tape in accordance with a preferred  
embodiment of the present invention;

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**Figure 7** is a flowchart representation of a process of correcting errors in a multi-track storage medium in accordance with a preferred embodiment of the present invention;

5        **Figure 8** is a flowchart representation of a process of error correction code decoding a block of data for a multi-track medium using a variable number of erasures in accordance with a preferred embodiment of the present invention; and

10       **Figure 9** is a block diagram of special-purpose hardware for performing error correction in an alternative embodiment of the present invention.

**DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT**

**Figure 1** is a diagram representing an overall view  
5 of a multi-track recording device (tape drive **100**) in  
accordance with a preferred embodiment of the present  
invention. The present invention provides a method,  
computer program product, and data processing system for  
correcting errors in a multi-track data storage medium.  
10 One commonly used multi-track data storage medium is  
magnetic tape. The embodiment herein disclosed utilizes  
magnetic tape as the physical data storage medium, but  
one of ordinary skill in the art will recognize that the  
present invention is applicable in conjunction with any  
15 physical data storage medium utilizing multiple tracks of  
data.

Tape drive **100** reads and writes data to/from  
magnetic tape **102**. Data buffer **104** acts as a temporary  
storage location for data read from or being written to  
20 magnetic tape **102**. Write circuitry **106** reads data from  
data buffer **104**, processes the data, and transmits the  
processed data to read/write head **108** for writing to  
magnetic tape **102**. Write circuitry **106**'s processing of  
the data includes encoding the data with an error  
25 correcting code, such as a Reed-Solomon code, and may  
include additional processes such as appending error-  
detecting codes such as CRC codes to the data.

Read circuitry **110** performs what is essentially the  
opposite transaction as write circuitry **106**. Read  
30 circuitry **110** decodes data read from magnetic tape **102** by

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read/write head **108**, correcting errors as necessary, and writes the data to data buffer **104**.

In a preferred embodiment of the present invention, tape drive **100** is associated with a host computer or  
5 network (not shown), and data buffer **104** is read from and written to by the host computer or by other devices (such as computers or network-connected peripherals). For example, a host computer may write data to data buffer **104**, which is then written by tape drive **100** to magnetic  
10 tape **102**.

The subject of the present invention is the error-correction decoding of data from a multi-track storage medium. Thus, the present invention is primarily concerned with the operation of read circuitry **110** as it  
15 decodes data stored on magnetic tape **102** that is encoded with an error-correcting code.

**Figure 2** is a block diagram depicting read circuitry in accordance with a preferred embodiment of the present invention. Note that the circuitry in **Figure 2** may also  
20 be used for performing tasks associated with write circuitry **106** in **Figure 1** or other tasks within tape drive **100**, as appropriate.

A processor **200** functions as the control center for read circuitry **110** (or tape drive **100**, generally, in one  
25 possible embodiment). Processor **200** communicates through memory **202** through bus system **204**. Memory **202** holds a set of instructions that is executed by processor **200** to carry out the processes of the present invention described in subsequent Figures. Also connected to  
30 device bus **202** is a read/write head interface **206**, which

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allows processor 200 to control the reading and writing of data to/from magnetic tape 102 via read/write head 108. Data buffer 104, which is preferably some type of random-access memory (RAM) is also connected to bus  
5 system 204 to allow processor 200 to read and write data to/from data buffer 104. In an alternative embodiment, memory 202 and data buffer 104 are combined into a single bank of memory.

Processor 200 executes a set of instructions located  
10 in memory 202. As used in this application, the term "instructions" is to be interpreted broadly so as to encompass a wide variety of functional descriptive material that enables the processor to execute the processes of the present invention. In the conventional  
15 sense, instructions are a series of commands, that when executed in sequence by the processor, cause the processor to perform the processes of the present invention. A machine language program or a program written in a high-level computer language, such as C or  
20 C++ would include instructions, in this conventional sense.

For the purposes of this document, however, "instructions" are also taken to include a set of facts and rules of inference that, when processed by processor  
25 200, cause processor 200 to follow a course of action that carries out the processes of the present invention. Such instructions could be written in a logic-programming or relational language such as Prolog. "Instructions" also include, for the purposes of this document,  
30 functions and expressions written in a functional

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programming language, such as Lisp. One of ordinary skill in the art will recognize that functional descriptive material of various other forms may be considered instructions for the purposes of the present document without departing from the scope and spirit of the present invention.

The depicted example in **Figure 2** and above-described hardware examples are not meant to imply architectural limitations. The actual hardware used to execute the processes of the present invention may vary.

Referring to **Figure 3**, a one-half inch wide length of magnetic tape **311** may contain up to 288 or more data tracks on multiple data stripes **312**. A thin film magnetic read head is shown in upper position **313** and lower position **314** to read data from data tracks **312**. If a tape read head has sixteen elements and, with movement of the head to multiple positions, each element can read nine tracks, then that magnetic read head could read 144 tracks. In order to read more tracks, such as 288 in the desired configuration, two data bands **315** and **316** are utilized. The tape head is movable to nine tracking positions in each of upper position **313** and lower position **314**. That is, with the tape head in position **313** it can read 144 tracks in data band **315** and in position **314** it can read 144 tracks in data band **316**.

In a preferred embodiment of the present invention, blocks of data are stored across tracks in encoded form using an error-correcting code, such as a Reed-Solomon code. This provides a level of data redundancy (in an information-theoretical sense) between tracks, such that

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if one or more of the tracks contains errors, redundant information in other tracks can be used to correct the error.

**Figure 4** is a graphic representation of how an error correcting code, such as a Reed-Solomon code, can correct errors in a multi-track data storage medium, in accordance with a preferred embodiment of the present invention. Block **400** is a block of data. Block **400** comprises four units (e.g., words, bytes, nybbles, etc.) of raw data. Using an error-correcting code, these four units of data are transformed into block **402**, which contains six units of encoded data.

The key to an error-correcting code is that to recover the original data, not all of the encoded data is needed. Thus, if some of the encoded data gets corrupted or lost, the original data may still be recoverable if enough units of the encoded data are intact. In a multi-track data storage medium, it makes sense to place each of the units of encoded data on separate physical tracks, since physical corruption of the media may be confined to particular physical locations on the tape. Thus, some tracks of a multi-track medium may become corrupted while others remain unaffected.

For example, in **Figure 4**, any four out of the six units of encoded data are all that are needed to recover the original data. Thus, if units **401** and **403** are corrupted, units **404**, **406**, **408**, and **410** can be decoded to form decoded block **412**, which is identical to the original block **400**.

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A careful examination of **Figure 4** reveals that there are two key pieces of information that are needed to reconstruct an original block of data from its encoded version. The first and most clearly needed piece of information that is needed is the encoded data itself. The second, not so clear, is the locations of the actual errors. For example, in **Figure 4**, we need to know that units **401** and **403** are corrupted before we can choose to decode the data using units **404**, **406**, **408**, and **410**.

It turns out that with many codes, the locations of the errors can be determined algorithmically, provided enough "good" (uncorrupted) data exists. In the case of a Reed-Solomon code, for instance, an extra unit of "good" data is needed in order to identify the location of an error.

Since magnetic tape and many other multi-track media store data and are read in linear sequential format, however, it is not possible to know with complete certainty where the errors in a given block of data are located. The present invention uses historical error correction data to make an "educated guess" as to which tracks are corrupted at any given location on the storage medium. Specifically, a preferred embodiment of the present invention selects a limited number of tracks with high past occurrence of errors to be treated as "erasures." Essentially, this means that these selected tracks are assumed to be corrupted and are ignored when the data is decoded.

What this means is that if one of these selected erasure tracks has an error occur on it at a particular

point, less "good" data will be needed for decoding, since there is no need to identify where the error on the erasure track has occurred. The trade-off for this increase in efficiency is that if an erasure track is actually uncorrupted at a particular point, the uncorrupted data (which otherwise would be used for decoding) will be wasted. Thus, a preferred embodiment of the present invention limits the number of designated erasure tracks to those considered most likely to contain an error.

**Figure 5** is a diagram illustrating how the processes of a preferred embodiment of the present invention may be applied to a multi-track data storage medium to maximize error-correcting capabilities. Chart **500** represents a length of multi-track magnetic tape. A plurality of tracks **502** span the width of the tape. At periodic locations along the length of the tape, blocks **504** of Reed-Solomon-encoded data are stored. Block **506**, for instance, is depicted as storing "n" units of Reed-Solomon encoded data (i.e., "n" Reed-Solomon coefficients).

Errors are present on the recording surface and are represented by black bars on the diagram. Error **510** is a small isolated error, whereas errors **512** are long portions of corrupted or erased data. At the end of the portion of tape, a checksum block **508** stores checksums, preferably some kind of cyclic redundancy check (CRC) value. Checksum block **508** can be used to identify data errors on tracks over a length of tape. Preferably,

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checksum blocks are present at periodic intervals along the length of the tape.

Checksum block 508 can detect that an error has occurred on a track over the length of tape, but it does not help in determining how extensive the errors are. In other words, checksum block 508 cannot be used to tell the difference between a small error such as error 510 and a large error such as errors 512.

What a preferred embodiment of the present invention does, however, to alleviate the situation is to calculate weights 516 for each track. These weights are preferably a measure of the number of errors corrected on each track as the track is read. In other words, in a preferred embodiment, each time an error on a given track is corrected, the weight for that track is increased. In this way the top "x" number of tracks in terms of highest weight can be designated as erasure tracks and thus ignored in the decoding process. Thus, long stretches of errors such as errors 512 will likely be treated as erasures, allowing more "good" data to be used for correcting isolated errors such as error 510.

As the storage medium is read from and the weights updated, the designated erasure tracks will change, depending on which tracks the most number of errors are occurring on at each particular position along the length of the storage medium. This allows a storage system to adapt to changing conditions as different physical locations along the medium are read. In a preferred embodiment of the present invention, these updates in

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erasure tracks are performed periodically, each time a checksum block is encountered.

In one embodiment of the present invention, all tracks that have contained errors at some point are  
 5 treated as erasures until the number of errors and erasures at some point on the medium is so large as to make the errors at that point uncorrectable. In such case, low-weight erasures are removed from the set of designated erasures until all of the errors can be  
 10 corrected.

**Figure 6** depicts a process of decoding one block of Reed-Solomon encoded data from a multi-track magnetic tape in accordance with a preferred embodiment of the present invention. Block **600** includes eight Reed-Solomon  
 15 coefficients (denoted "n" in the diagram, thus n=8). Block **600** represents two units of data (i.e., "m", the size of the original amount of data, is 2). Two tracks, and thus two of the coefficients, coefficients **602** and **608**, are designated as erasures (i.e., "e" the number of erasures, is 2). Coefficient **602**, which is treated as an  
 20 erasure, is corrupted. Coefficients **604** and **606**, which are not on erasure tracks, are also corrupted (i.e., "t" the number of errors [other than erasures], is 2). It is well known in the art that in the case of a Reed-Solomon  
 25 code, if the following inequality holds, then the original data can be recovered:

$$2t + e \leq n - m.$$

In this case,  $2t + e = 6 = n - m$ , so the inequality is satisfied. Thus, the errors may be corrected. In  
 30 addition, the weights for tracks 5 and 6 (corresponding

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to coefficients 604 and 606) will be increased, as errors were corrected on these tracks.

Figure 7 is a flowchart representation of a process of correcting errors in a multi-track data storage medium in accordance with a preferred embodiment of the present invention. A block of encoded data is read from the storage medium (in this case, a tape) (step 700). The block is decoded, while treating certain tracks designated as erasure tracks as containing corrupted data (step 702).

If any errors were corrected in decoding the block (step 704:Yes), the weight values for the tracks containing the errors are updated (step 706). If the end of a length of tape (containing a cyclic redundancy check or other suitable checksum) has not yet been reached (step 708:No), the process cycles to step 700 for further data reading.

If the end of the length has been reached (step 708:Yes), cyclic redundancy checks (or other suitable checksums) are calculated for the length of tape read (step 710). If there are no tracks that do not match (i.e., no errors occurred on the length of tape) (step 712:No), the process cycles to step 700 to continue reading data.

If, however, errors are detected (step 712:Yes), the "N" tracks with highest weight that contained errors in the previous length are identified (step 714). Those tracks are then designated as the new erasure tracks (step 716).

**Figure 8** is a flowchart representation of a process of error correction code decoding a block of data for a multi-track medium using a variable number of erasures in accordance with a preferred embodiment of the present invention. The process described in **Figure 8** starts with a number of erasures being already defined. For example, all tracks that have previously contained errors may be designated erasure tracks at the beginning of the process described in **Figure 8**.

10 First, the number of designated erasures is checked to see if it exceeds the "order of the code" (step 800). In other words, the number of erasures is checked to see if it exceeds that amount which the code will allow to be decoded (the  $n-m$  in the  $2t-e \leq n-m$  equation described  
15 earlier in this document). If so (step 800:Yes), then the "x" highest-weight erasures are then designated current set of erasures and passed to the decoder (decoding software or hardware or a combination of both), with "x" being some number less than or equal to  $n-m$   
20 (step 802). If not (step 800:No), then the current set of erasures is simply passed to the decoder (step 804).

Next, the decoder attempts to decode the block of data from the multitrack medium (step 806). If the decoding was successful (step 808:Yes), then the process  
25 ends. If the decoding was not successful (step 808:No), a different "x" is tried or different coefficients are used for the decoding (step 810) and the process cycles to step 802, so as to (eventually) make an exhaustive search of all the decoding possibilities until the block  
30 is successfully decoded.

Although the processes of the present invention have been described as being executed by an embedded stored-program computer system as in **Figure 2**, the processes of the present invention need not be carried out by such hardware. For example, **Figure 9** is a block diagram of "hard-wired" (special-purpose) hardware for carrying out the processes described herein. The apparatus described in **Figure 9** may be implemented in digital logic using conventional synthesis techniques.

Correction history registers **900** store weights for each track that has been corrected. These weights are fed into priority selector **902**, which selects the "X" highest weight erasures according to "X" input **904**, which is derived from decode logic **906**. Decode logic **906** decodes tape data **908** using the "X" highest-weight erasures as determined by priority selector **902**. Any adjustments to "X" necessary to ensure complete decoding of tape data **908** are made by transmitting a new "X" value to priority selector **902** through "X" input **904**. Properly decoded data is sent to output **910**, from which the data may be written to data buffer **104** (**Figure 1**).

It is important to note that while the present invention has been described in the context of a fully functional data processing system, those of ordinary skill in the art will appreciate that the processes of the present invention are capable of being distributed in the form of a computer readable medium of instructions and a variety of forms and that the present invention applies equally regardless of the particular type of signal bearing media actually used to carry out the

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distribution. Examples of computer readable media include recordable-type media such a floppy disc, a hard disk drive, a RAM, CD-ROMs, and transmission-type media such as digital and analog communications links.

5       The description of the present invention has been presented for purposes of illustration and description, and is not intended to be exhaustive or limited to the invention in the form disclosed. Many modifications and variations will be apparent to those of ordinary skill in  
10 the art. The embodiment was chosen and described in order to best explain the principles of the invention, the practical application, and to enable others of ordinary skill in the art to understand the invention for various embodiments with various modifications as are  
15 suited to the particular use contemplated.